

SKEMA JAWAPAN

MODUL PENINGKATAN MURID TINGKATAN 5

TAHUN 2022/2023

MATEMATIK TAMBAHAN
KERTAS 2

2 JAM DAN 30 MINIT

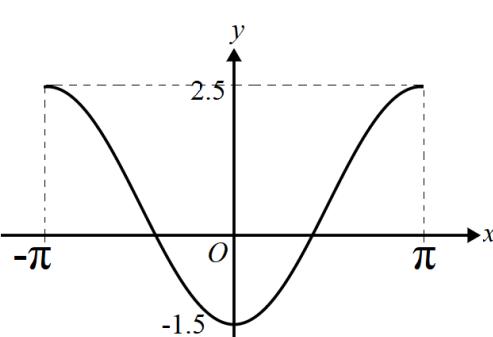
JANGAN BUKA SKEMA PEMARKAHANINI SEHINGGA DIBERITAHU

| 1 | Skema Permarkahan | Sub Markah | Jumlah Markah |
|----------|--|-----------------------|--------------------------|
| (a) | $2x + 2y + 16 = 36 \text{ atau } \sqrt{x^2 + y^2} = 2\sqrt{13} \quad P1$ $x = 10 - y \text{ setara } P1$ $\sqrt{(10-y)^2 + y^2} = 2\sqrt{13} \text{ setara } K1$ $y^2 - 10y + 24 = 0$ $(y-6)(y-4) = 0 \text{ setara } K1$ $y = 6, y = 4 \quad N1$ $x = 4, x = 6 \quad N1$ $(4+8)+6$ $18 \text{ cm} \quad N1$ | 7 | 7 |

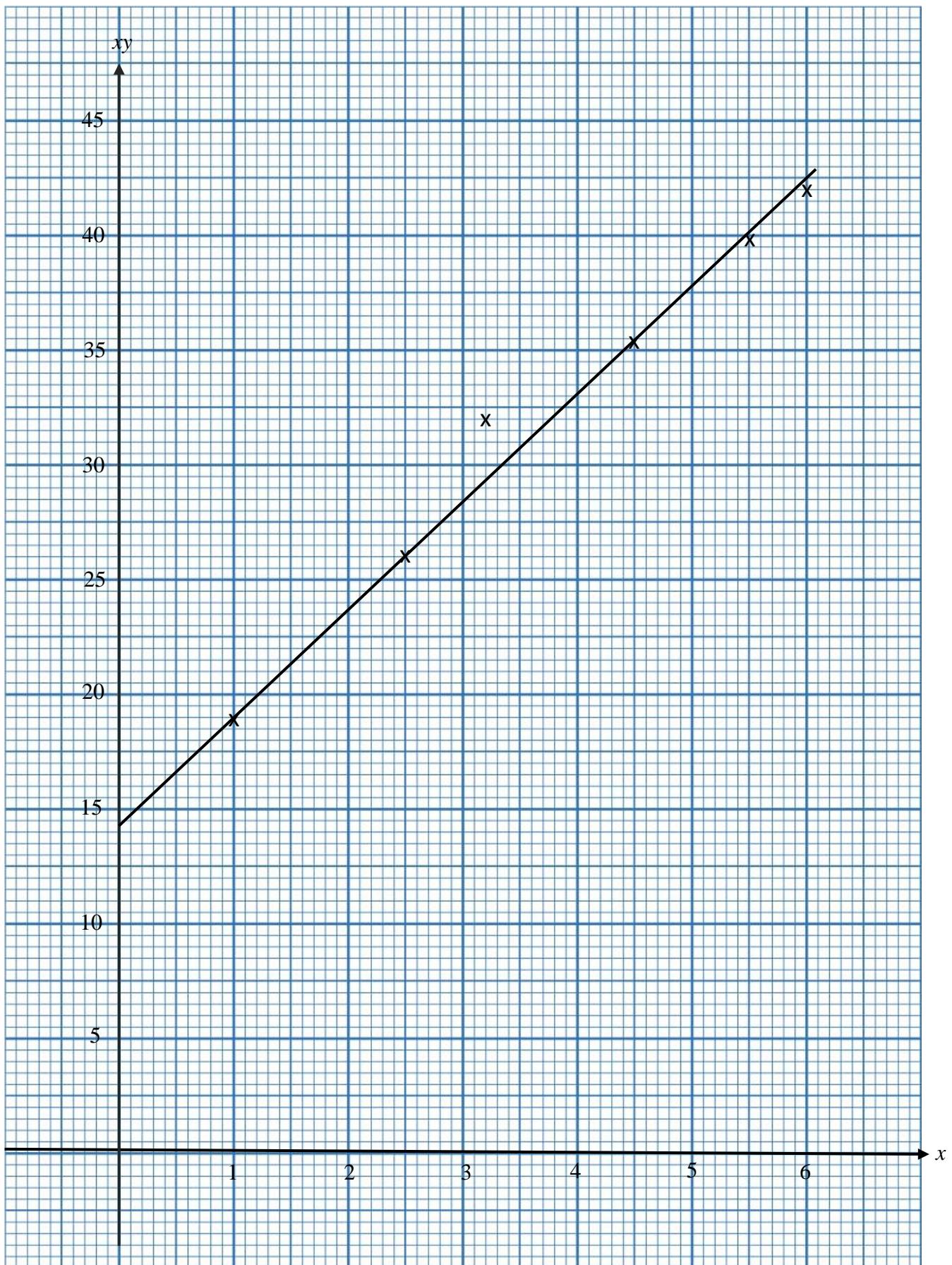
| 2 | Skema Permarkahan | Sub Markah | Jumlah Markah |
|----------|--|-------------------|----------------------|
| (a) | $\frac{dy}{dx} = 8(2x-3)^3$ $\frac{dy}{dx} = 8(2(1)-3)^3 \quad \text{K1 ganti nilai } x \text{ dalam fungsi kecerunan}$ $\frac{dy}{dx} = -8$ $m_1 = -8$ $-8 \times m_2 = -1 \quad \text{K1}$ $m_2 = \frac{1}{8}$ $y = \frac{1}{8}x - \frac{25}{8} \quad \text{N1}$ | 3 | |
| (b) | $3 - \frac{3}{x^2} = 0 \quad \text{K1}$ $3x^3 - 3 = 0$ $x^3 = 1$ $x = 1$ $m = 1 \quad \text{N1}$ | 2 | 7 |
| (c) | $\frac{d^2y}{dx^2} = 3 + \frac{6}{x^3}$ $\frac{d^2y}{dx^2} = 3 + \frac{6}{(1)^3} \quad \text{K1}$ $\frac{d^2y}{dx^2} > 0 \text{ minimum N1}$ | 2 | |

| 3 | Skema Permarkahan | Sub Markah | Jumlah Markah |
|----------|--|-------------------|----------------------|
| (a) | $m = \tan \theta$ $m = \tan 135^\circ$ atau setara K1 $m = -1$ N1 $y - 4 = -1(x + 2)$ atau setara K1 $y = -x + 2$ N1 | 4 | |
| (b) | $m_{CD} = 1$ $y - 0 = 1(x - 4) / 0 = 4 + c$ $y = x - 4$ N1 $x - 4 = -x + 2$ K1 $x = 3$ $y = 3 - 4$ $y = -1$ $C(3, -1)$ N1 | 3 | 8 |
| (c) | $x = 3$ N1 | 1 | |

| 4 | Skema Permarkahan | Sub Markah | Jumlah Markah |
|----------|---|-------------------|----------------------|
| (a) | $hk(x) = 2\left(\frac{x}{p}\right) + 3 \quad K1$ $h^{-1}(x) = \frac{px - 3p}{2} \quad K1 \text{ banding}$ $h^{-1}(x) = x - 3$ $p = 2 \quad N1$ | 3 | |
| (b)(i) | $k^2(x) = p(px) \quad K1 \text{ ganti } p = 2$ $k^2(x) = 4x \quad N1$ | 2 | 7 |
| (b)(ii) | $k(x) = 2x$ $k^2(x) = 4x$ $k^3(x) = 9x$ $k^4(x) = 16x$ tulis $k^3(x)$ atau $k^4(x) \quad K1$ $k^n(x) = n^2 x \quad N1$ | 2 | |

| 5 | Skema Permarkahan | Sub Markah | Jumlah Markah |
|-----|---|------------|---------------|
| (a) | $\frac{1+\cos x}{\sin x} = \cot \frac{x}{2}$ $\frac{1+2\cos^2 \frac{x}{2}-1}{2\sin \frac{x}{2} \cos \frac{x}{2}} \quad K1$ $\frac{\cos \frac{x}{2}}{\sin \frac{x}{2}} \quad K1$ $\cot \frac{x}{2} \quad N1$ | 4 | |
| (b) |  <p>Bentuk graf sinus P1 $\frac{1}{2}$ kitaran P1 Amplitud P1 anjakan keatas P1</p> | 8 4 | |

| 6 | Skema Permarkahan | Sub Markah | Jumlah Markah |
|----------|---|-------------------|----------------------|
| (a) | <p>Rujuk graf</p> <p>Graf garis lurus xy melawan x dilukis K1</p> <ul style="list-style-type: none"> ▪ Paksi-paksi betul dan skala seragam <p>Sekurang-kurangnya 5 titik diplot dengan betul N1</p> <p>Garis penyuaian terbaik N1</p> | 3 | |
| (b)(i) | $xy = \sqrt{rx} + \frac{r}{t} \quad \text{P1}$ $r = 21.16 \quad \text{N1 (ikut jawapan daripada nilai kecerunan calon)}$ $t = 1.459 \quad \text{N1 (ikut jawapan daripada nilai } r \text{ calon)}$ $y = 9.06 \quad \text{N1 (ikut jawapan daripada nilai } r \text{ calon)}$ | 4 | 7 |



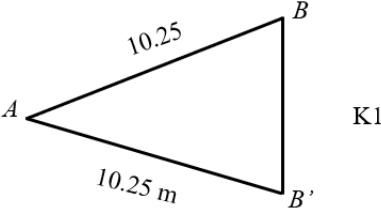
| 7 | Skema Permarkahan | Sub Markah | Jumlah Markah |
|---------|--|------------|---------------|
| (a)(i) | $\overrightarrow{AP} = \frac{3}{4}(\overrightarrow{AO} + \overrightarrow{OB})$ tulis Hukum K1 $\overrightarrow{AP} = -\frac{3}{4}\underline{u} + \frac{3}{4}\underline{v}$ $\overrightarrow{OP} = \underline{u} + \frac{3}{4}\underline{v} - \frac{3}{4}\underline{u}$ N1 $\overrightarrow{OP} = \frac{1}{4}(\underline{u} + 3\underline{v})$ Terbukti N1 | 3 | 7 |
| (a)(ii) | $\overrightarrow{PQ} = -\frac{1}{4}\underline{u} - \frac{3}{4}\underline{v} + \frac{2}{3}\underline{w}$ N1 | 1 | |
| (b) | $\overrightarrow{BC} = \overrightarrow{BA} + \overrightarrow{AO} + \overrightarrow{OC}$ Tulis hukum K1 $-\frac{1}{4}\underline{u} - \frac{3}{4}\underline{v} + \frac{2}{3}\underline{w} = \frac{6}{5}(-\underline{v} + \underline{w})$ K1 $\underline{w} = \frac{27\underline{v} - 15\underline{u}}{32}$ N1 | 3 | |

| 8 | Skema Permarkahan | Sub Markah | Jumlah Markah |
|---------|---|---------------|------------------|
| (a)(i) | $\frac{dy}{dx} = 3x^2 \quad \text{atau} \quad \frac{dy}{dx} = -2x \quad \text{K1}$ $-2 \quad \text{N1}$ <p>Lengkung $y = -x^2 + 2$ N1</p> | 3 | |
| (a)(ii) | $\int_0^1 -x^2 + 2 \, dx - \int_0^1 x^3 \, dx \quad \text{K1}$ $\left[-\frac{x^3}{3} + 2x \right]_0^1 - \left[\frac{x^4}{4} \right]_0^1 \quad \text{K1}$ $\left(\left[-\frac{(1)^3}{3} + 2(1) \right] - \left[-\frac{(0)^3}{3} + 2(0) \right] \right) - \left(\left[\frac{(1)^4}{4} \right] - \left[\frac{0^4}{4} \right] \right) \quad \text{K1}$ $\frac{17}{12} \text{ unit}^2 \quad \text{N1}$ | 4 | 10 |
| (b) | $\pi \int_0^k 2x \, dx = 9\pi$ $\left[\frac{2x^2}{2} \right]_0^k = 9 \quad \text{K1}$ $(k^2) - (0) = 9 \quad \text{K1}$ $k = 3 \quad \text{N1}$ | 3 | |

| 9 | Skema Permarkahan | Sub Markah | Jumlah Markah |
|--------|---|------------|---------------|
| (a) | <p>Luas Poligon Sekata</p> $= \frac{1}{2} \times r^2 \times \sin 30^\circ \times 12$ $= 3r^2$ <p>P1</p> <p>Luas Kawasan Tidak Berlorek</p> $=(2 \times \text{Luas tembereng}) + \text{Luas Segitiga}$ $= 0.1810r^2 + \frac{1}{4}r^2$ <p>K1</p> $= 0.431r^2$ <p>N1</p> <p>Luas Kawasan Berlorek</p> $=\text{Luas Poligon} - \text{Luas kawasan tidak berlorek}$ $=3r^2 - 0.431r^2$ <p>K1</p> $= 2.569r^2 \text{ cm}^2$ <p>N1</p> | 5 | |
| (b)(i) | <p>Panjang sisi $\times 8$</p> $\frac{\text{BS}}{\sin 30} = \frac{10}{\sin 75}$ <p>K1</p> $\text{BS} = 5.176$ $\therefore = 5.176 \times 8$ $= 41.408 \text{ cm}$ <p>N1</p> <p>Panjang Lengkok Berlorek</p> $= r\theta$ $= 10(60 \times \frac{\pi}{180})$ $= 10.47 \text{ cm}$ <p>N1</p> <p>Panjang Lengkok Berlorek</p> $= 10.47 \times 8$ $= 83.76 \text{ cm}$ <p>N1</p> <p>Perimeter Kawasan Berlorek</p> $= 41.408 + 83.76$ $= 125.168 \text{ cm}$ <p>N1</p> | 10 | |

| 10 | Skema Permarkahan | Sub Markah | Jumlah Markah |
|-----------|--|-------------------|----------------------|
| (a)(i) | $x - 10 = 90 - x \quad \text{K1}$ $x = 50$ $d = 40 \quad \text{N1}$ $T_{20} = 10 + (20-1)(40) \quad \text{K1}$ $770 \quad \text{N1}$ | 4 | |
| (a)(ii) | $S_8 = \frac{8}{2} [2(10) + (8-1)(40)] \quad \text{K1}$ $1200 - 770$ $430 \quad \text{N1}$ | 2 | 10 |
| (c) | $850 = 10 + (n-1)40 \quad \text{K1}$ $n = 22$ $\text{RM}10 \times 22 \quad \text{K1}$ $\text{RM}220 \quad \text{N1}$ <p>Cukup , kerana tidak melebihi RM250 N1</p> | 4 | |

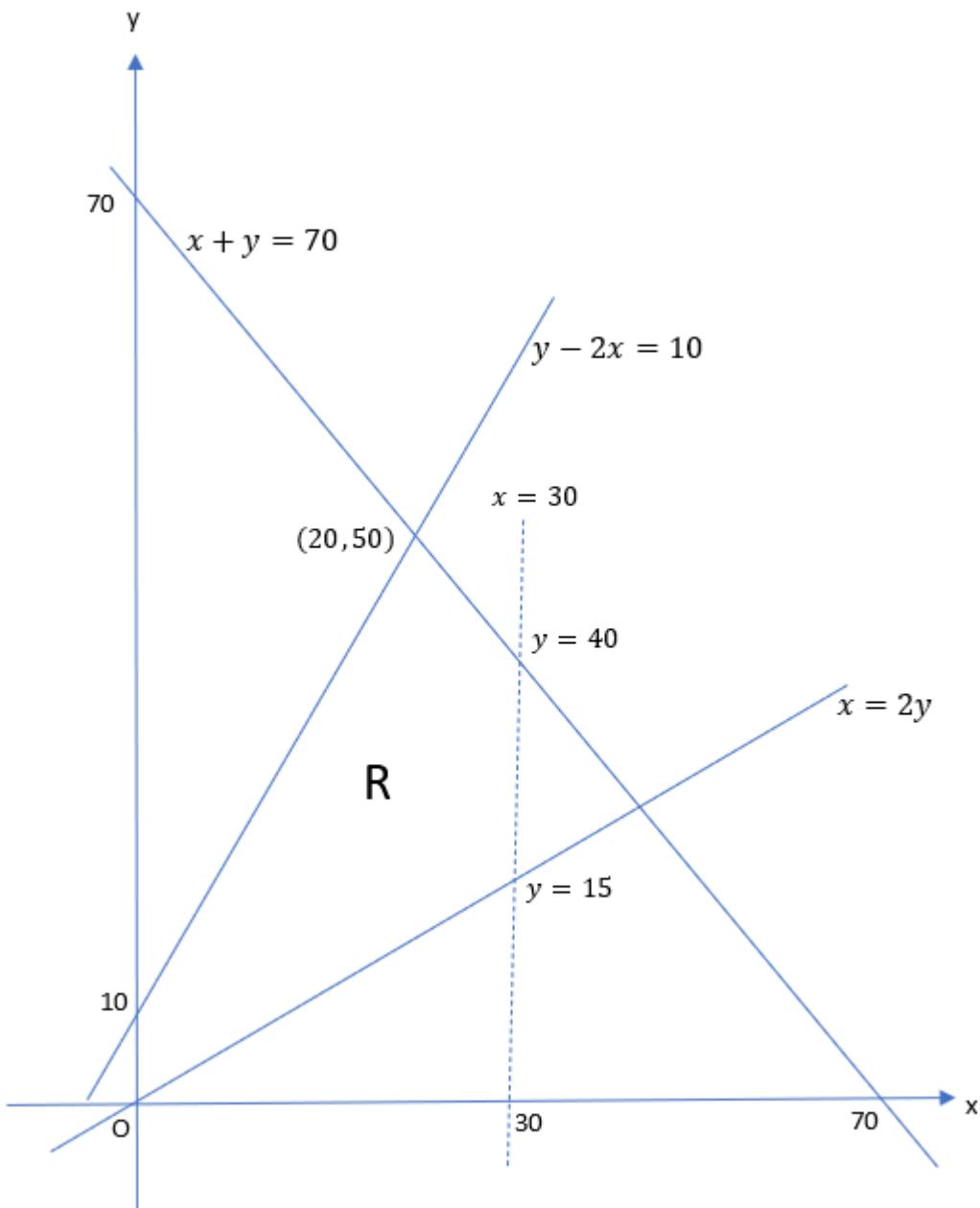
| 11 | Skema Permarkahan | Sub Markah | Jumlah Markah |
|-----------|---|-------------------|----------------------|
| (a)(i) | $5q = 4$ $q = \frac{4}{5}$ $p = \frac{1}{5} \quad \text{N1}$ $n\left(\frac{1}{5}\right)\left(\frac{4}{5}\right) = 4$ $n = 25 \quad \text{N1}$ | 3 | |
| (a)(ii) | ${}^{25}C_2 \left(\frac{1}{5}\right)^2 \left(\frac{4}{5}\right)^{23} \quad \text{K1}$ $0.0708 \quad \text{N1}$ | 2 | 10 |
| (b)(i) | $P\left(\frac{3.5 - 4.5}{1.1} < Z \leq \frac{6.5 - 4.5}{1.1}\right) \quad \text{K1}$ $0.7837 \quad \text{N1}$ | 2 | |
| (b)(ii) | $P(Z < m) = 0.02 \text{ or } P(Z > m) = 0.98$ $Z = 2.054 \quad \text{N1}$ $-2.054 = \frac{m - 4.5}{1.1} \quad \text{K1}$ $2.241 \text{ kg} \quad \text{N1}$ | 3 | |

| 12 | Skema Permarkahan | Sub Markah | Jumlah Markah |
|----------|--|------------|---------------|
| (a) (i) | $AB = \sqrt{10^2 + 2.26^2} \quad \text{or} \quad AF = \sqrt{10^2 + 6.26^2}$ $AB = 10.25 \quad AF = 11.80 \quad \text{K1}$ $4^2 = 11.80^2 + 10.25^2 - 2(11.80)(10.25) \cos\angle BAF \quad \text{K1}$ $\angle BAF = 19.30^\circ \quad \text{N1}$ | 3 | |
| (a)(ii) | $\frac{11.80}{\sin \angle DCG} = \frac{4}{\sin 19.30} \quad \text{K1}$ $\angle DCG = 77.17 \quad \text{N1}$ | 2 | |
| (a)(iii) | $s = \frac{11.80 + 7.21 + 13.83}{2} \quad \text{K1}$ $s = 16.42$ $\text{Luas } DFG = \sqrt{16.42(16.42 - 11.80)(16.42 - 7.21)(16.42 - 13.83)} \quad \text{K1}$ $= 42.54 \quad \text{N1}$ | 3 | 10 |
| (b) |  $\angle BAB' = 25.66^\circ \quad \text{NI}$ | 2 | |

| 13 | Skema Permarkahan | Sub Markah | Jumlah Markah |
|-----------|---|-------------------|----------------------|
| (a)(i) | $\frac{720}{Q_0} \times 100 = 120 \quad \text{K1}$ $Q_0 = \text{RM } 600.00 \quad \text{N1}$ | | |
| (a)(ii) | $126.3 = \frac{(120 \times 144) + (x \times 108) + (150 \times 72) + (108 \times 36)}{(144 + 108 + 72 + 36)} \quad \text{K1}$ $= 125 \quad \text{N1}$ | 4 | |
| (b) | $I_{\frac{22}{20}} = \frac{(108 \times 144) + (125 \times 108) + (157.5 \times 72) + (108 \times 36)}{(144 + 108 + 72 + 36)} \quad \text{K1}$ <p>Semua Indeks harga $\frac{2022}{2020}$ betul K1</p> <p>123 N1</p> <p>Jumlah perbelanjaan pada tahun 2022 meningkat 23% berbanding tahun 2020 N1</p> | 4 | 10 |
| (c) | $\frac{Q_1}{4000} \times 100 = 123 \quad \text{K1}$ $Q_1 = \text{RM } 4920.00 \quad \text{N1}$ | 2 | |

| 14 | Skema Permarkahan | Sub Markah | Jumlah Markah |
|-----|---|------------|---------------|
| (a) | <p>ganti $t = 0$</p> $(0)^2 - 6(0) + 8 \quad \text{K1}$ $8 \text{ ms}^{-1} \quad \text{N1}$ | 2 | |
| (b) | $a = 0$ $\frac{dV}{dt} = 2t - 6 \quad \text{K1}$ $0 = 2t - 6$ $t = 3$ $v = (3)^2 - 6(3) + 8 \quad \text{K1}$ $-1 \text{ ms}^{-1} \quad \text{N1}$ | 3 | |
| (c) | $v < 0$ $t^2 - 6t + 8 < 0 \quad \text{N1}$  $2 < t < 4 \quad \text{N1}$ | 3 | 10 |
| (d) | $\int_0^2 t^2 - 6t + 8 \, dt + \left \int_2^4 t^2 - 6t + 8 \, dt \right $ $\left[\frac{t^3}{3} - \frac{6t^2}{2} + 8t \right]_0^2 + \left[\left[\frac{t^3}{3} - \frac{6t^2}{2} + 8t \right]_2^4 \right] \quad \text{K1}$ <p>ganti had untuk mendapatkan nilai K1</p> $8.67 \text{ m} / \frac{26}{3} \text{ m} \quad \text{N1}$ | 3 | |

| 15 | Skema Permarkahan | Sub Markah | Jumlah Markah |
|-----------|--|-------------------|----------------------|
| (a) | I $x + y \leq 70$N1 II $x \leq 2y$N1 III $y - 2x \leq 10$N1 Atau Setara | 3 | |
| (b) | Rujuk graf: -Lukis dengan betul sekurang-kurangnya satu garis lurus daripada *ketaksamaan melibatkan x dan yK1 -Lukis dengan betul semua *garisan lurus daripada *ketaksamaan melibatkan x dan y ...N1 -Tanda R dengan betul N1 <u>Nota:</u> Terima garis putus-putus dan garis penuh. | 3 | 10 |
| (c) | (i) $15 \leq y \leq 40$N1 (ii) Koordinat $(20, 50)$N1 Ganti mana-mana titik dalam *kawasan berlorek dalam $10x + 20y$K1 RM1200N1 | 4 | |



PERATURAN PEMARKAHAN TAMAT